Permutations of $\{1, \ldots, n\}$ and related permanents

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Abstract

In this talk we introduce recent results on permutations of $\{1, \ldots, n\}$. For example, we show that for any positive integer n there is a unique permutation $\pi \in S_n$ such that all the numbers $k + \pi(k)$ $(k = 1, \ldots, n)$ are powers of two.

We also mention some divisibility properties of the permanent

$$\operatorname{per}[i^{j-1}]_{1 \le i,j \le n} = \sum_{\sigma \in S_n} \prod_{i=1}^n i^{\sigma(i)-1}$$

as well as related applications to groups.

We also introduce some open conjectures of the speaker, one of which states that for any integer n > 6 there is a permutation $\pi \in S_n$ such that

$$\sum_{k=1}^{n-1} \frac{1}{\pi(k) + \pi(k+1)} = 1.$$